

Statistics

Lecture 21



Feb 19-8:47 AM

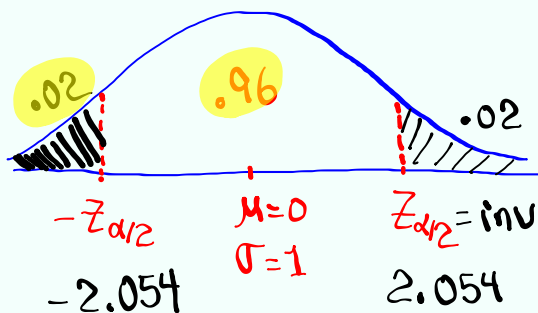
(SG 21)

Find $\pm Z_{\alpha/2}$ for 96% Confidence level.

Middle Area = .96

$1 - \alpha = .96$

$\alpha = .04$ Sig. level



$$Z_{\alpha/2} = \text{invNorm}(.98, 0, 1) = 2.054$$

Nov 17-10:38 AM

I surveyed 275 students and 16% of them had a full-time job while going to school.

$$n = 275 \Rightarrow x = n\hat{p} = 275(.16) = \boxed{44}$$

$$\hat{p} = .16 \quad \text{if decimal} \rightarrow \text{Round-up}$$

Find 90% Conf. interval for the prop. of all students that have a full-time job.

C-level: .9

$$\boxed{.12 < p < .20}$$

1-Prop Z Int

$$x = 44$$

$$n = 275$$

C-level: .9

$\hat{p}$ was 2-dec.

So we round to 2-dec

we are 90% confident

that between 12% & 20% of all students have a full-time job.

$$E = \frac{.20 - .12}{2} = \boxed{.04}$$

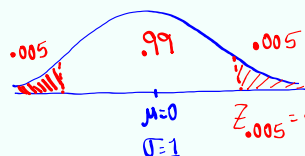
$$\hat{p} = \frac{.20 + .12}{2} = \boxed{.16}$$

Nov 17-10:43 AM

What is the minimum Sample Size needed if we wish to have 99% Conf. interval for the prop. of all students that have a full-time job if we want error not to exceed 5%? $n = ?$ C-level: .99, $E = .05$

$$\hat{p} = .16, \hat{q} = 1 - \hat{p} = .84$$

$$n = \hat{p}\hat{q} \left(\frac{Z_{\alpha/2}}{E} \right)^2 = (.16)(.84) \left(\frac{2.576}{.05} \right)^2 = 356.739 \dots \approx \boxed{357}$$



$$Z_{.005} = \text{invNorm}(.995, 0, 1) = \boxed{2.576}$$

Suppose $\hat{p}$ & $\hat{q}$ are unknown

$$n = .25 \left(\frac{Z_{\alpha/2}}{E} \right)^2 = .25 \left(\frac{2.576}{.05} \right)^2 = 663.5776$$

SG 21 ✓

$$\approx \boxed{664}$$

Nov 17-10:51 AM

Estimating Population Mean μ S6 22

Answer $\dots < \mu < \dots$

Format $\bar{x} - E < \mu < \bar{x} + E$

$\uparrow$ Sample Mean $\uparrow$ Margin of error
 Point-estimate

Case I: σ Known

$E = Z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}$

C.V. $Z_{\alpha/2} \rightarrow$ in UNorm

Conf. interval $\rightarrow$ Z Interval
 inpt: Stats

Nov 17-11:02 AM

Given: $n=35$, $\bar{x}=82$, $\sigma=10$

Find 98% conf. interval for pop. mean.

Since σ is known, $78.068 < \mu < 85.932$

Use Z Interval

STAT
TESTS
Z Interval

inpt: Stats

$\sigma=10$
 $\bar{x}=82$
 $n=35$
 C-level: .98
Calculate

Since point-estimate $\bar{x}$ is a whole #, we round to whole #.

$78 < \mu < 86$

$E = \frac{86 - 78}{2} = [4]$ $\bar{x} = \frac{86 + 78}{2} = [82]$

Nov 17-11:07 AM

I randomly selected 30 students, their mean age was 32.5 yrs. $n=30$
 $\bar{x}=32.5$

Find $\text{No C-level} \rightarrow .95$ Conf. interval for the mean age of all students assuming standard dev. of ages of all students is 8.5 yrs.

$$\sigma=8.5 \quad 29.458 < \mu < 35.542$$

σ is known $\rightarrow$ Z Interval

inpt: Stats

$$\sigma=8.5$$

$$\bar{x}=32.5$$

$$n=30$$

$$\text{C-level}=.95$$

Since point-estimate $\bar{x}$ is in 1-dec, we round to 1-dec.

$$29.5 < \mu < 35.5$$

$$E = \frac{35.5 - 29.5}{2} = 3$$

Calculate

we are 95%.

Confident that the mean age of all students is between 29.5 & 35.5 yrs.

$$\bar{x} = \frac{35.5 + 29.5}{2} = 32.5$$

Nov 17-11:14 AM

A sample of 40 nurses, their mean monthly salary was \$6375.

$$n=40, \bar{x}=6375$$

$$\text{C-level}=.99$$

Find 99% Conf. interval for the mean salary of all nurses if it is known that standard deviation of salaries of all nurses is \$450. $\sigma=450$

$$6192 < \mu < 6558$$

σ known $\rightarrow$ Z Interval

$$E = \frac{6558 - 6192}{2}$$

$$= 183$$

inpt: Stats

$$\sigma=450$$

$$\bar{x}=6375 \text{ (whole \#)}$$

$$n=40$$

$$\text{C-level}=.99$$

Calculate

$$\bar{x} = \frac{6558 + 6192}{2}$$

$$= 6375$$

Nov 17-11:27 AM

Estimating Population Mean μ S6 22	
Answer	$... < \mu < ...$
Format	$\bar{x} - E < \mu < \bar{x} + E$
	$\uparrow$ Sample Mean Point-estimate $\uparrow$ Margin of error
Case I: σ Known	Case II: σ unknown
$E = Z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}$	$E = t_{\alpha/2} \cdot \frac{s}{\sqrt{n}}$
C.V. $Z_{\alpha/2} \rightarrow \text{invNorm}$	C.V. $t_{\alpha/2} \rightarrow \text{invT}$ $df = n - 1$
Conf. interval $\rightarrow$ Z Interval inpt: Stats	Conf. interval $\rightarrow$ T Interval inpt: STATS

Nov 17-11:02 AM

Given $n=15$ $\bar{x}=86$ $s=12$

Find 90% Conf. interval for population mean

Since σ is unknown $< \mu <$

we use T Interval

inpt Stats

$\bar{x}=86$ (whole) $81 < \mu < 91$

$s=12$

$n=15 \rightarrow df = n - 1$
14

C-level = .9

Calculate

Nov 17-11:41 AM

I randomly Selected 12 exams, their mean was 84.5 with standard dev. of 8.2.

$$n=12, \bar{x}=84.5, S=8.2$$

Find no c-level $\rightarrow .95$ Conf. interval for mean Score of all exams.

$$79.3 < \mu < 89.7$$

σ is unknown

$\Rightarrow$ T Interval

inpt: STATS

$$\bar{x}=84.5 \text{ (1-dec.)}$$

$$S=8.2$$

$$n=12$$

$$C\text{-level: } .95$$

Calculate

$$E = \frac{89.7 - 79.3}{2} = 5.2$$

$$\bar{x} = \frac{89.7 + 79.3}{2} = 84.5$$

$$df = n - 1 = 11$$

Nov 17-11:47 AM

I took a Sample of 10 Students. Here are their ages:

23 25 18 20 30

32 38 19 24 30

use calc to find $\bar{x}$ & S. Round to whole #.

$$\bar{x} = 26$$

$$S = 6$$

Find 99% Conf. interval for the mean age of all Students.

$$20 < \mu < 32$$

σ unknown $\rightarrow$ T Interval

inpt: Stats

$$\bar{x} = 26 \text{ (whole)}$$

$$S = 6$$

$$n = 10$$

$$C\text{-level} = .99$$

Calculate

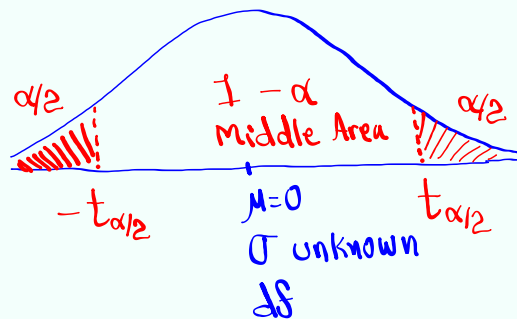
$$E = \frac{32 - 20}{2} = 6$$

$$\bar{x} = \frac{32 + 20}{2} = 26$$

Nov 17-11:57 AM

t - Dist:

- 1) It is symmetric, bell-shape with total area = 1.
- 2) $\mu=0$, σ unknown
- 3) It comes with degrees of freedom.
 df

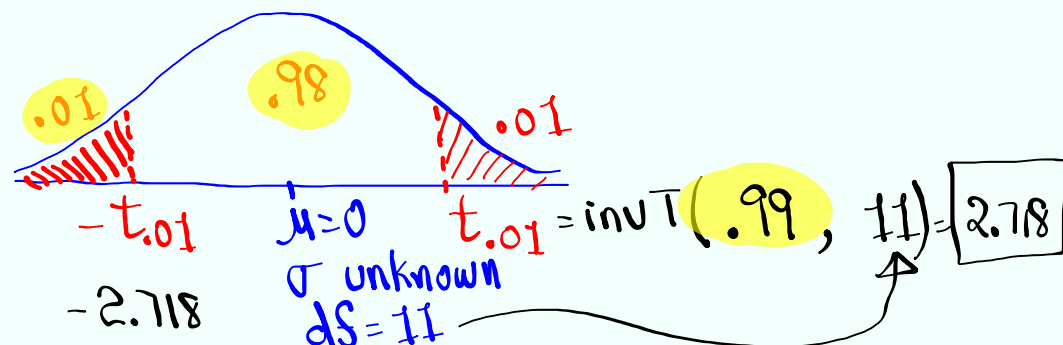


How to Find $t_{\alpha/2}$:
use
 $\text{invT}(\text{Left Area}, df)$

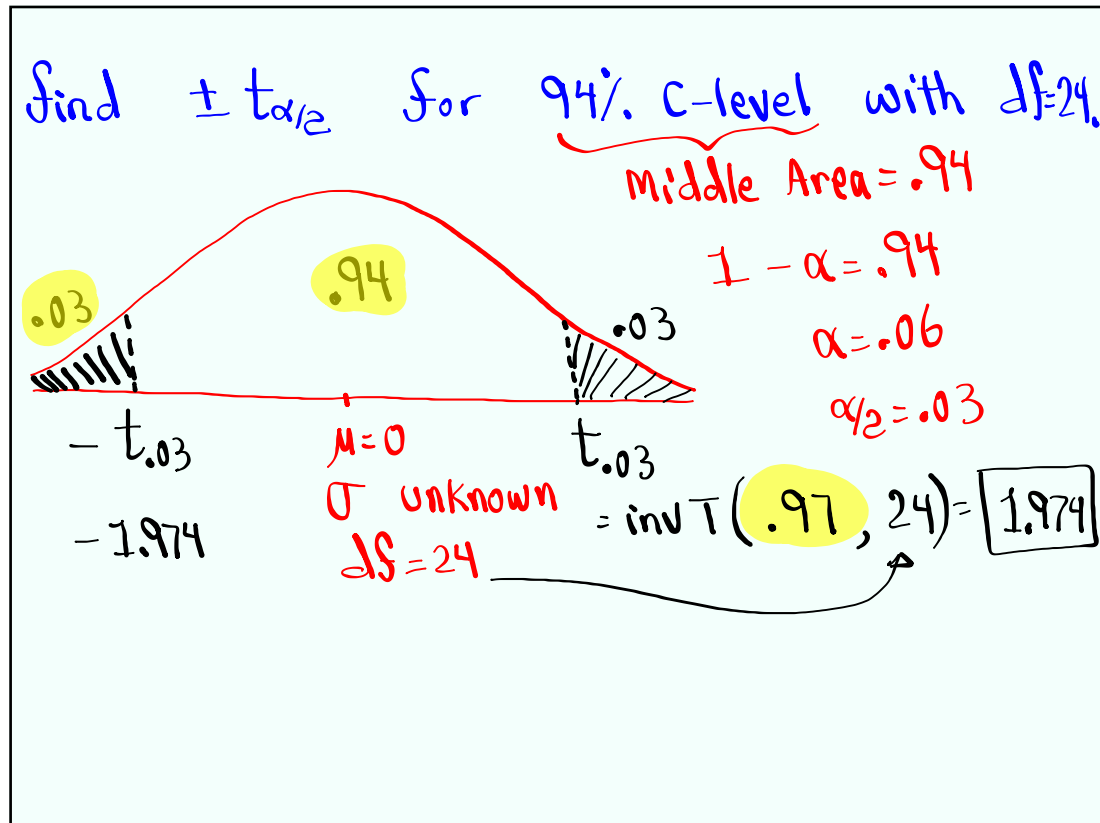
Nov 17-12:05 PM

Find $t_{.01}$ with $df = 11$.

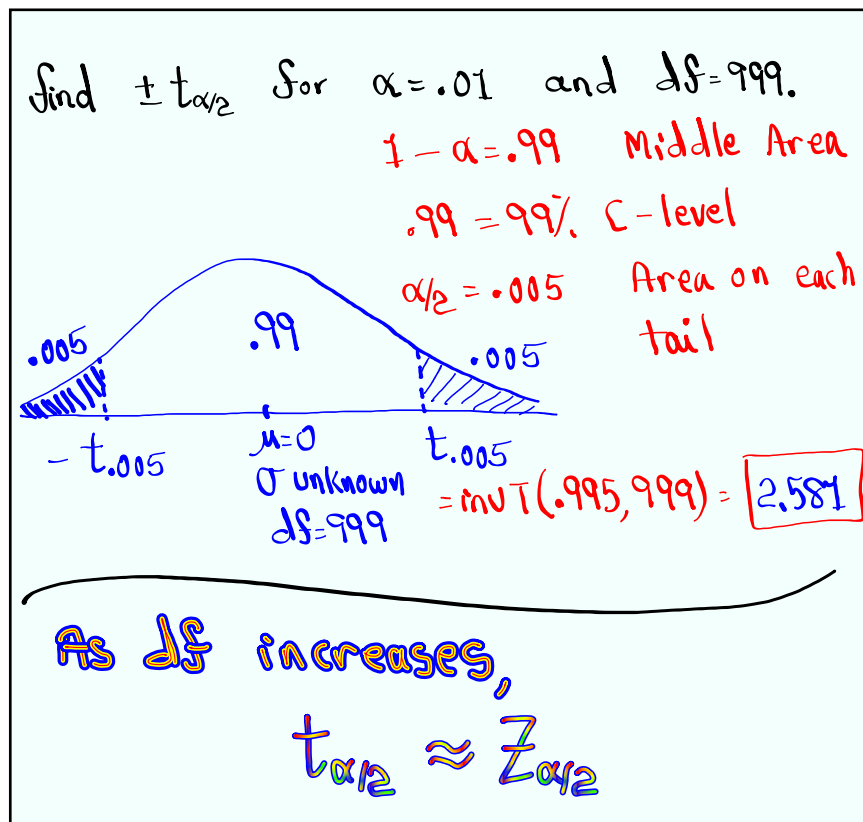
$\rightarrow$ Right-Tail Area
 $\alpha/2 = .01 \rightarrow \boxed{\alpha = .02}$
 $1 - \alpha = .98 \rightarrow \text{C-level: } 98\%$



Nov 17-12:10 PM



Nov 17-12:15 PM



Nov 17-12:19 PM

What is degrees of freedom?

It is a value given to us by the problem or can be determined by certain methods by topics.

20 students, I bring 20 donuts.

You can have one donut.

First student	20 choices (20 Donuts)
Second "	19 " (19 Donuts)
Third "	18 " (18 Donuts)
⋮	
Last student	0 choice (1 Donut)

$$df = 19$$

Nov 17-12:25 PM

7 clean shirts, you only wear a clean shirt

Monday 7 choices

Tuesday 6 "

wednesday 5 "

⋮
Sunday 0 choice (1 clean shirt Available)

$$df = 7 - 1 = \boxed{6}$$

Nov 17-12:30 PM